

# Cooperation

## Emergence in complex systems

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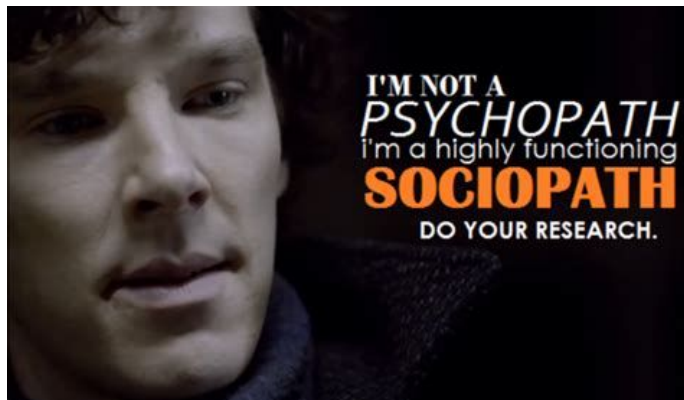
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Ecole Normale Supérieure

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# Why altruism?



Economist: :(  
(Game Theory // Nash equilibrium)

Biologist: :) (?)  
(Evolutionary Game Theory // ESS,  
which resist *mutant* strategies)

# Golden Balls



# The Prisoner's dilemma



		Prisoner A	
		<i>C</i>	<i>D</i>
Prisoner B	<i>C</i>	$(-1, -1)$	$(-20, 0)$
	<i>D</i>	$(0, -20)$	$(-10, -10)$

Years in prison faced by both prisoner's depending on their actions (cooperate or defect on the other)





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# The Prisoner's dilemma

Benefit of help:  $b$

Cost of helping someone else:  $c$

Benefit of mutual cooperation:  $b - c > 0$

		Chooser	
		$A$	$R$
Signaler	$C$	$(b - c, b - c)$	$(-c, b)$
	$D$	$(b, -c)$	$(0, 0)$

Payoffs for a typical cooperative dilemma

→ *The only ESS for the prisoner's dilemma is  $(D, D)$*

So why do we manage to cooperate ?



One game: the social optimum (C,C) is not reached. What if games are *repeated* with a certain probability?

<https://ncase.me/trust/>

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Note your score.

And your total score is...

39

which is pretty good! (the lowest & highest possible scores are 7 and 49, respectively)

So who were these strange characters you just played against?



**COPYCAT:** Hello! I start with Cooperate, and afterwards, I just copy whatever you did in the last round. Meow



**ALWAYS CHEAT:**  
*the strong shall eat the weak*



**ALWAYS COOPERATE:**  
Let's be best friends! <3



**GRUDGER:** Listen, pardner. I'll start cooperatin', and keep cooperatin', but if y'all ever cheat me, I'LL CHEAT YOU BACK 'TIL THE END OF TARNATION.



**DETECTIVE:** First: I analyze you. I start: Cooperate, Cheat, Cooperate, Cooperate. If you cheat back, I'll act like Copycat. If you never cheat back, I'll act like Always Cheat, to exploit you. Elementary, my dear Watson.

Now, what if these characters were to play...

...against each other? →

# Tournament

What about when players enter in indefinitely repeated interactions (probability of ending  $\mu$ )? How do you think will win the "tournament":

- A) A pure defector, who always plays  $D$  — and thus exploits others' generosity
- B) A pure cooperator, who always plays  $C$  — and thus benefits from repetition when encountering other cooperators (as they gain  $b - c$  for several rounds)
- C) "Tit-for-tat": a player who starts of by playing  $C$  and then just repeats the other players' last interaction.
- D) Some other more complex strategy, which figures out others' player strategy in the first few rounds, using a neural network

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# Reciprocal cooperation

Indefinite repetition can allow reciprocal cooperation to emerge ("do unto others as you would have do unto you") — as shown by an actual tournament organized by R. Axelrod [Trivers, 1971, Axelrod and Hamilton, 1981].

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Refinement: indirect reciprocity and reputation

[Nowak and Sigmund, 1998, Panchanathan and Boyd, 2003]

Non-human animal examples:



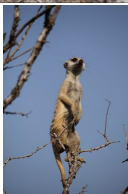
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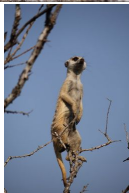
What explanation would you invoke for the following behavior?



# Explanations for helpful behavior

Explanations seen up until now:

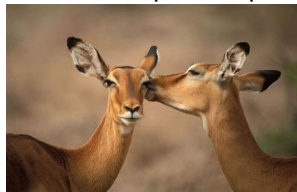
Kin altruism:  $-C_i, +B_o$  ( $rB_o > C_i$ )



Mutualism or by-product cooperation:  $+B_i, +B_o$



Reciprocal cooperation:  $+B_i$  because help is recip.,  $+B_o$ .

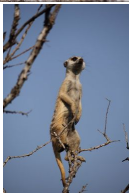




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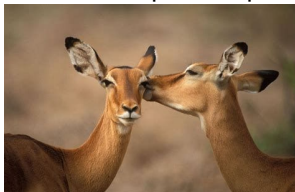
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- We help unrelated individuals
- Including strangers we will likely never meet again
- We take into account mistakes and/or attenuating circumstances
- We don't value efficiency [Borum et al., 2020]
- We do not keep track of favours with certain partners [Hoffman et al., 2015]
- We sometimes obscure our good deeds [Hoffman et al., 2018]
- We value and trust others more when they appear uncalculating, most or uninterested in material gains
- We don't simply trust based on behavior in a similar game, or reciprocate help with help, but instead make a wide-series of cross-inferences, and hold a "general" reputation

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Next session: signaling. NB: Actually Tit for Tat is not an ESS!

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